# Cube with two different walls with variable meshgrid

#### MATLAB / Octave files:

```
t04Cube2wFB.m;
fTC2SSa.m
fSolRadTiltSurf.m
fReadWeather.m
```

#### Objectives:

- Obtain variable meshgrids.
- Study the influence of the space discretization on the model dynamics.

## 1 Physical analysis and mathematical model

The mathematical model is similar to Tutorial no. 3. The main difference is that the wall can be discretized in a number of meshes given by the user in lines 8 and 9:

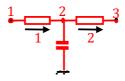
```
8 - nc = 3; % number of concrete meshes
9 - ni = 2; % number of insulation meshes
10 - dt = 3600 % [s] simulation time step
```

## 2 Implementation

The discretization of the concrete wall and insulation is done in:

```
38 - Gc = lamc/wc*Sc; Cc = Sc*wc*rhoccc; %concrete
39 - Gcm = 2*nc*Gc*ones(1,2*nc); %meshed concrete
40 - Ccm = Cc/nc*mod(0:2*nc-1,2);
41
42 - Gi = lami/wi*Si; Ci = Si*wi*rhoici; %insulation
43 - Gim = 2*ni*Gi*ones(1,2*ni); %meshed insulation
44 - Cim = Ci/ni*mod(0:2*ni-1,2);
```

There are *n* meshes, each one formed by two resistances and a capacity.



The two conductances are equal and their value is the double of the conductance of the mesh. The first node does not have a capacity; the second node has the capacity of the mesh; the third node is not in the mesh (it is in the next mesh).

The whole model has the conductance matrix:

```
76 - G = diag([Gwo Gcm Gim GLW Gwi Ggi Ggs 2*Gg Gv Kp]');
```

and the capacity matrix:

if the capacities of air and glass are considered, or

```
80 - % C = diag([Ccm Cim 0 0 Ca Cg]);
81 C = diag([Ccm Cim 0 0 0 0]);
```

if they are not considered.

### 3 Numerical experiments and discussion

#### 3.1 Number of meshes

Neglect the air capacity:

Use the same discretization as in Tutorial 3.

```
7 - Kp = 1e4; % P-controller gain: large for precision
8 - nc = 1; % number of concrete meshes
9 - ni = 1; % number of insulation meshes
10 - dt = 5 % [s] simulation time step
```

Compare the results with those from tutorial 3.

Change the discretization:

and discuss its influence on the maximum simulation time step.

Consider the heat capacity of the air:

```
80 - C = diag([Ccm Cim 0 0 Ca Cg]);
81 % C = diag([Ccm Cim 0 0 0 0]);
```

Discuss the maximum simulation time step.

#### 3.2 Time constants

Find the time constants,

```
[\min(-1./\operatorname{eig}(As)) \max(-1./\operatorname{eig}(As))]
```

for 1 mesh and 3 meshes of the concrete layer, with and without indoor air heat capacity. Observe the values in different situations.

#### 3.3 Controller amplification

On line 6

```
6 - Kp = 1e-1; %P-controller gain: large for precision
```

change the controller proportional constant Kp: 1e4, 1e3, 1e2, 1e1, 1e0, 1e-1. Discuss the significance of these values and their connection with the time step dt.

# 3.4 Implicit Euler integration

# Change the script

```
105 - for k = 1:n-1

106 - th(:,k+1) = (eye(nth) + dt*As)*th(:,k) + dt*Bs*u(:,k);

107 - end
```

in order to integrate with implicit Euler. Discuss the results.