## Combinatorial Circuits

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- Until now we have seen how to compute logical functions using Boole algebra
- Now, we will show how to implement these logical functions into digital circuits


## Logical gates and circuits

Logical gates are the basic building blocks of digital circuits :


A logical signal is a physical mean of transmitting a truth value from one place to another. We represent them as wires.

From the outside, a logical circuit shows input and output signals: every output signal is a function of the input signals (possibly a subset of).

## Assembly rules - combinational circuits

Combinatorial Logical Circuits (CLC) can be defined recursively:

- as a gate
- as a wire
- as a side-by-side juxtaposition of 2 CLCs
- by connecting the outputs of a CLC to inputs of another CLC
- by connecting inputs of a CLC together.

This definition forbids:

- to make cycles, because they introduce undefined behaviors, eg

- to connect outputs with each other (what if an output is 1 and the other is 0 ?)


## Blackboard Example

## Decoder

A decoder $n$ to $2^{n}$ is a circuit with:

- $n$ inputs $e_{i}$, encoding an integer $\left(e_{n-1} \ldots e_{0}\right)_{2}$;
- $2^{n}$ outputs $s_{i}$, indexed from 0 à $2^{n}-1$.


## The only active output line is $s_{\left(e_{n-1} \ldots e_{0}\right)_{2}}$.

E.g., a 3-to-8 decoder


## Blackboard example: Building a 2-to-4 decoder from its truth table.

## Multiplexer

A $2^{n}$ to 1 multiplexer is a circuit with:

- $2^{n}$ inputs $e_{i}$ indexed from 0 to $2^{n}-1$;
- $n$ selection lines, encoding the integer $\left(c_{n-1} \ldots c_{0}\right)_{2}$;
- 1 output $s$.

When selection lines for the value $\left(c_{n-1} \ldots c_{0}\right)_{2}$,

$$
s=e_{\left(c_{n-1} \ldots c_{0}\right)_{2}}
$$

E.g., a $2^{1}$ to 1 multiplexer


## Blackboard example: Building the 2 to 1 multiplexer from its truth table.

## Blackboard example: 1 to 2 demultiplexer

## (Another) Multiplexer

An $k$-bits $2^{n}$-to- 1 multiplexer is a circuit with:

- $k \cdot 2^{n}$ inputs and $n$ selection lines;
- $k$ output signals

It selects $k$ signals among $k \cdot 2^{n}$ input signals
Ex: 8-bits 2-to-1 multiplexer:


